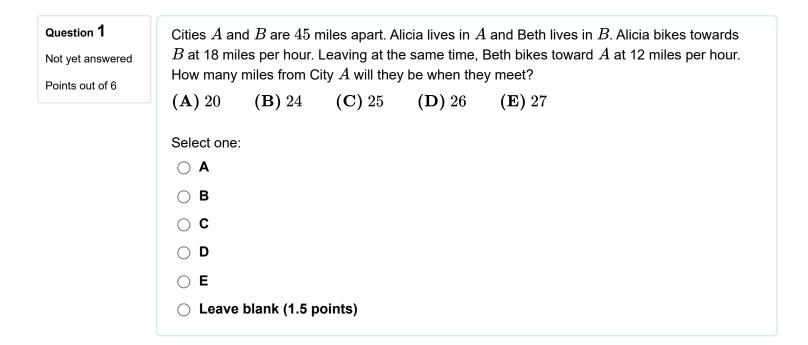
2023 AMC 12A

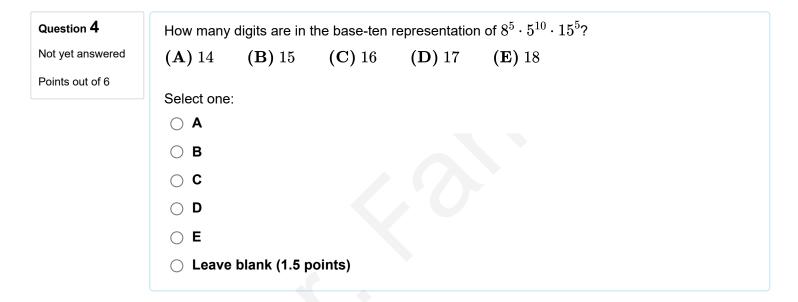
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Question 2	The weight of $\frac{1}{3}$ of a large pizza together with $3\frac{1}{2}$ cups of orange slices is the same as the
Points out of 6	weight of $\frac{3}{4}$ of a large pizza together with $\frac{1}{2}$ cup of orange slices. A cup of orange slices
	weighs $rac{1}{4}$ of a pound. What is the weight, in pounds, of a large pizza?
	(A) $1\frac{4}{5}$ (B) 2 (C) $2\frac{2}{5}$ (D) 3 (E) $3\frac{3}{5}$
	Select one:
	○ A
	○ B
	○ C
	○ D
	○ E
	○ Leave blank (1.5 points)

Question 3	How mar	ny positive p	erfect square	s less than 20	023 are divisible by $5?$	
Not yet answered	(A) 8	(B) 9	(C) 10	(D) 11	(E) 12	
Points out of 6						
	Select on	ne:				
	A (
	ОВ					
	⊖ с					
	○ D					
	○ E					
	⊖ Leav	ve blank (1.	5 points)			



Question 5 Not yet answered

Points out of 6

Janet rolls a standard 6-sided die 4 times and keeps a running total of the numbers she rolls. What is the probability that at some point, her running total will equal 3?

(A)
$$\frac{2}{9}$$
 (B) $\frac{49}{216}$ (C) $\frac{25}{108}$ (D) $\frac{17}{72}$ (E) $\frac{13}{54}$
Select one:
A
B
C
D
E
Leave blank (1.5 points)

Question 6 Not yet answered	Points A and B positive difference				oint of \overline{AB} is $(6,2).$ What is the $3?$
Points out of 6	(A) $2\sqrt{11}$	(B) $4\sqrt{3}$	(C) 8	(D) $4\sqrt{5}$	(E) 9
	Select one:				
	○ A				
	ОВ				
	○ C				
	○ D				
	○ E				
	○ Leave blan	k (1.5 points)			

Not yet answered

Points out of 6

A digital display shows the current date as an 8-digit integer consisting of a 4-digit year, followed by a 2-digit month, followed by a 2-digit date within the month. For example, Arbor Day this year is displayed as 20230428. For how many dates in 2023 will each digit appear an even number of times in the 8-digital display for that date?

(A) 5	(B) 6	(C) 7	(D) 8	(E) 9
Select on	e:			
○ A				
○ B				
○ C				
○ D				
○ E				
🔿 Leav	ve blank (1.	5 points)		

Question 8

Not yet answered

Points out of 6

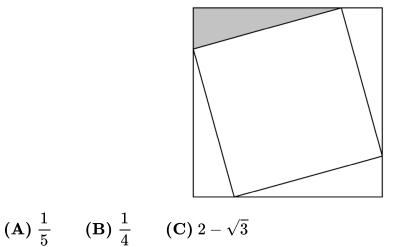
Maureen is keeping track of the mean of her quiz scores this semester. If Maureen scores an 11 on the next quiz, her mean will increase by 1. If she scores an 11 on each of the next three quizzes, her mean will increase by 2. What is the mean of her quiz scores currently?

(A) 4	(B) 5	(C) 6	(D) 7	(E) 8
Select on	e:			
○ A				
⊖ В				
○ C				
○ D				
○ E				
🔿 Leav	ve blank (1.	5 points)		

Not yet answered

Points out of 6

A square of area 2 is inscribed in a square of area 3, creating four congruent triangles, as shown below. What is the ratio of the shorter leg to the longer leg in the shaded right triangle?



(A) $\frac{1}{5}$ (B) $\frac{1}{4}$ (C) $2 - \sqrt{2}$ (D) $\sqrt{3} - \sqrt{2}$ (E) $\sqrt{2} - 1$

Select one:

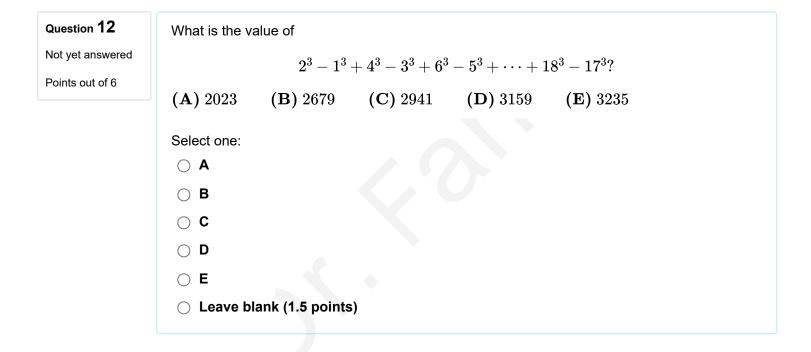
A
B
C

 \bigcirc D

- E
- Leave blank (1.5 points)

Question 10	Positive rea	I numbers x :	and y satisfy	$y^3=x^2$ and	$(y-x)^2=4y^2$. What is $x+y$?	
Not yet answered	(A) 12	(B) 18	(C) 24	(D) 36	(E) 42	
Points out of 6						
	Select one:					
	○ A					
	○ B					
	⊖ с					
	○ D					
	○ E					
	○ Leave	blank (1.5 pc	oints)			

Question 11 Not yet answered	What is the	e degree measu	ure of the acu	te angle formed	by lines with slopes 2 and $rac{1}{3}$?	
Points out of 6	(A) 30	(B) 37.5	(C) 45	(D) 52.5	(E) 60	
	Select one	:				
	 ○ B ○ C ○ D 					
) E	blank (1.5 poi	nto)			



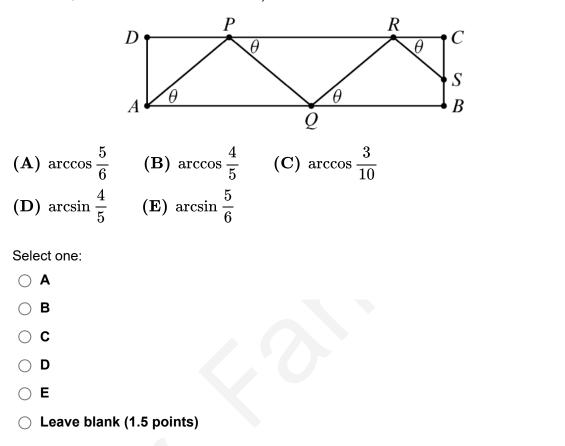
Question 13 Not yet answered Points out of 6	Although th of games w right-hande	nere were twi von by left-ha	ce as many ri nded players here were no	ght-handed p $ m was~40\%$ mc	ed every other participant exactly once. players as left-handed players, the number pre than the number of games won by ambidextrous players.) What is the total
	(A) 15	(B) 36	(C) 45	(D) 48	(E) 66
	Select one:	:			
	○ A				
	ОВ				
	⊖ с				
	O D				
	○ E				
	⊖ Leave	blank (1.5 p	oints)		

Question 14 Not yet answered	How many complex numbers satisfy the equation $z^5=\overline{z}$, where \overline{z} is the conjugate of the complex number z ?
Points out of 6	(A) 2 (B) 3 (C) 5 (D) 6 (E) 7
	Select one:
	○ B
	○ c
	○ D
	○ E
	 Leave blank (1.5 points)

Not yet answered

Points out of 6

Usain is walking for exercise by zigzagging across a 100-meter by 30-meter rectangular field, beginning at point A and ending on the segment \overline{BC} . He wants to increase the distance walked by zigzagging as shown in the figure below (APQRS). What angle $\theta \ \angle PAB = \angle QPC = \angle RQB = \cdots$ will produce in a length that is 120 meters? (This figure is not drawn to scale. Do not assume that he zigzag path has exactly four segments as shown; there could be more or fewer.)



Question 16	Consider the set of complex numbers z satisfying $ 1+z+z^2 =4.$ The maximum value of
Not yet answered Points out of 6	the imaginary part of z can be written in the form $\frac{\sqrt{m}}{n}$, where m and n are relatively prime positive integers. What is $m + n$?
	(A) 20 (B) 21 (C) 22 (D) 23 (E) 24
	Select one:
	\bigcirc A
	○ B
	○ c
	○ D
	○ E
	○ Leave blank (1.5 points)

Not yet answered

Points out of 6

Flora the frog starts at 0 on the number line and makes a sequence of jumps to the right. In any one jump, independent of previous jumps, Flora leaps a positive integer distance m with probability $\frac{1}{2^m}$.

What is the probability that Flora will eventually land at 10?

(A)
$$\frac{5}{512}$$
 (B) $\frac{45}{1024}$ (C) $\frac{127}{1024}$ (D) $\frac{511}{1024}$ (E) $\frac{1}{2}$

Select one:

A (

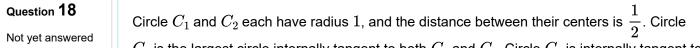
○ B

○ C

O D

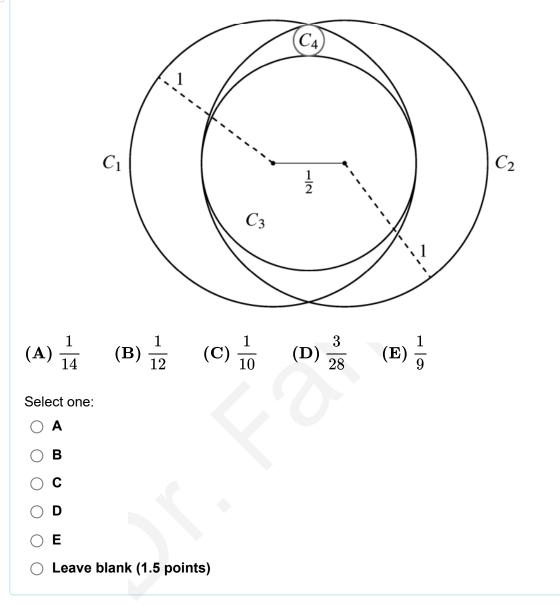
○ E

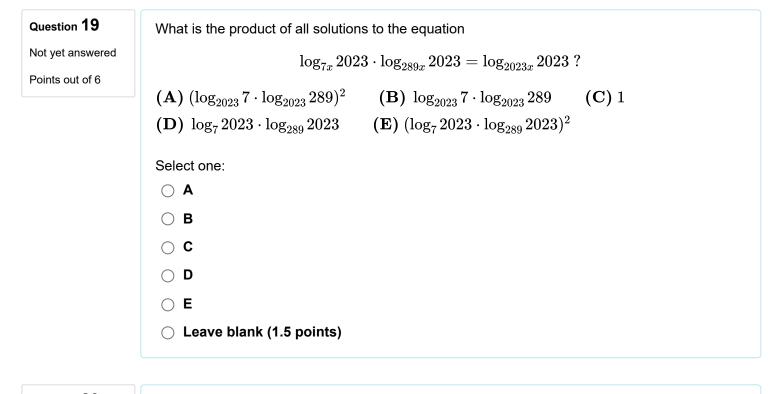
○ Leave blank (1.5 points)



Points out of 6

 C_3 is the largest circle internally tangent to both C_1 and C_2 . Circle C_4 is internally tangent to both C_1 and C_2 and externally tangent to C_3 . What is the radius of C_4 ?





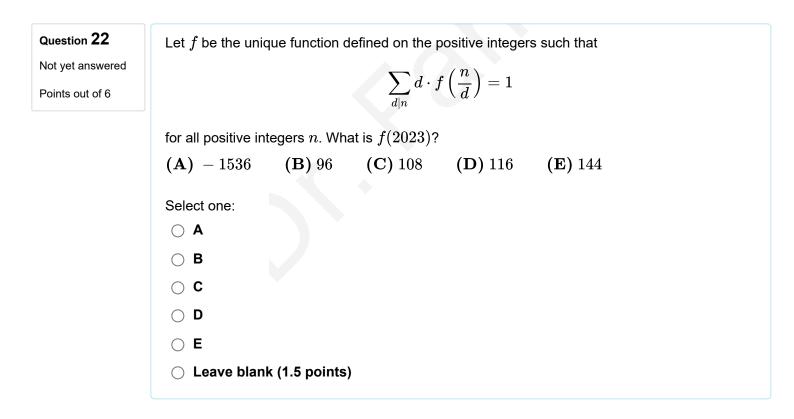
Question 20 Rows 1, 2, 3, 4, and 5 of a triangular array of integers are shown below. Not yet answered Points out of 6 1 1 1 Each row after the first row is formed by placing a 1 at each end of the row, and each interior entry is 1 greater than the sum of the two numbers diagonally above it in the previous row. What is the units digits of the sum of the 2023 numbers in the 2023rd row? **(B)** 3 **(C)** 5 **(D)** 7 **(E)** 9 **(A)** 1 Select one: ○ A О В ○ C O D ○ E C Leave blank (1.5 points)

Not yet answered

Points out of 6

If A and B are vertices of a polyhedron, define the *distance* d(A, B) to be the minimum number of edges of the polyhedron one must traverse in order to connect A and B. For example, if \overline{AB} is an edge of the polyhedron, then d(A, B) = 1, but if \overline{AC} and \overline{CB} are edges and \overline{AB} is not an edge, then d(A, B) = 2. Let Q, R, and S be randomly chosen distinct vertices of a regular icosahedron (regular polyhedron made up of 20 equilateral triangles). What is the probability that d(Q, R) > d(R, S)?

(A) $\frac{7}{22}$	(B) $\frac{1}{3}$	(C) $\frac{3}{8}$	(D) $\frac{5}{12}$	(E) $\frac{1}{2}$
Select one:				
○ A				
⊖ В				
⊖ с				
○ D				
○ E				
○ Leave b	lank (1.5 po	ints)		



How mar	ny ordered p	airs of positi	ive real num	bers (a,b) satisfy the equation
		(1 +	(2a)(2+2b))(2a+b)=32ab?
(A) 0	(B) 1	(C) 2	(D) 3	(\mathbf{E}) an infinite number
Select or	ie:			
A (
<u>о</u> В				
Ŭ				
) E				
	ve blank (1.	5 points)		
	(A) 0 Select or ○ A ○ B ○ C ○ D ○ E	 (A) 0 (B) 1 Select one: A B C D E 	(1 + (A) 0 (B) 1 (C) 2 Select one: ○ A ○ B ○ C ○ D ○ E	 (A) 0 (B) 1 (C) 2 (D) 3 Select one: A B C D E

Question 24 Not yet answered Points out of 6	Let K be the number of sequences A_1, A_2, \ldots, A_n such that n is a positive integer less than or equal to 10, each A_i is a subset of $\{1, 2, 3, \ldots, 10\}$, and A_{i-1} is a subset of A_i for each i between 2 and n , inclusive. For example, $\{\}, \{5,7\}, \{2,5,7\}, \{2,5,7\}, \{2,5,7\}, \{2,5,7\}, \{2,5,7\}, \{2,5,7\}, \{2,5,7,9\}$ is one such sequence, with $n = 5$. What is the remainder when K is divided by 10?
	(A) 1 (B) 3 (C) 5 (D) 7 (E) 9
	Select one:
	ightarrow A $ ightarrow$
	ОВ
	○ c
	\bigcirc D
	○ E
	 Leave blank (1.5 points)

Not yet answered

Points out of 6

There is a unique sequence of integers $a_1, a_2, \cdots, a_{2023}$ such that

$$an 2023x = rac{a_1 an x + a_3 an^3 x + a_5 an^5 x + \cdots + a_{2023} an^{2023} x}{1 + a_2 an^2 x + a_4 an^4 x + \cdots + a_{2022} an^{2022} x}$$

whenever an 2023x is defined. What is a_{2023} ?

(A)
$$-2023$$
 (B) -2022 (C) -1 (D) 1 (E) 2023
Select one:
 \bigcirc A
 \bigcirc B
 \bigcirc C
 \bigcirc D
 \bigcirc E

○ Leave blank (1.5 points)